

平方根の有理化と加減 解答と解説

[1] [解答] (1) $6\sqrt{2}$ (2) 0 (3) $2\sqrt{6}$ (4) $4\sqrt{3}$

$$(1) \sqrt{32} + \frac{4}{\sqrt{2}} = 4\sqrt{2} + \frac{4 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} \\ = 4\sqrt{2} + \frac{4\sqrt{2}}{2} \\ = 4\sqrt{2} + 2\sqrt{2} \\ = 6\sqrt{2}$$

$$(2) \frac{12}{\sqrt{3}} - \sqrt{48} = \frac{12 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} - 4\sqrt{3} \\ = \frac{12\sqrt{3}}{3} - 4\sqrt{3} \\ = 4\sqrt{3} - 4\sqrt{3} \\ = 0$$

$$(3) \frac{\sqrt{54}}{2} + \sqrt{\frac{3}{2}} = \frac{3\sqrt{6}}{2} + \frac{\sqrt{3}}{\sqrt{2}} \\ = \frac{3\sqrt{6}}{2} + \frac{\sqrt{3} \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} \\ = \frac{3\sqrt{6}}{2} + \frac{\sqrt{6}}{2} \\ = 2\sqrt{6}$$

$$(4) 3\sqrt{12} - \frac{15}{\sqrt{3}} + \sqrt{27} = 3 \times 2\sqrt{3} - \frac{15 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} + 3\sqrt{3} \\ = 6\sqrt{3} - \frac{15\sqrt{3}}{3} + 3\sqrt{3} \\ = 6\sqrt{3} - 5\sqrt{3} + 3\sqrt{3} \\ = 4\sqrt{3}$$

[2] [解答] (1) $6\sqrt{2}$ (2) $-\sqrt{3}$ (3) $\sqrt{6}$ (4) $6\sqrt{6}$

$$(1) \frac{8}{\sqrt{2}} + \sqrt{8} = \frac{8 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} + 2\sqrt{2} \\ = 4\sqrt{2} + 2\sqrt{2} \\ = 6\sqrt{2}$$

$$(2) \sqrt{48} - \frac{15}{\sqrt{3}} = 4\sqrt{3} - \frac{15 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}}$$

$$= 4\sqrt{3} - 5\sqrt{3} \\ = -\sqrt{3}$$

$$(3) \sqrt{\frac{2}{3}} + \frac{4}{\sqrt{6}} = \frac{\sqrt{2}}{\sqrt{3}} + \frac{4}{\sqrt{6}} \\ = \frac{\sqrt{2} \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} + \frac{4 \times \sqrt{6}}{\sqrt{6} \times \sqrt{6}} \\ = \frac{\sqrt{6}}{3} + \frac{2\sqrt{6}}{3} \\ = \sqrt{6}$$

$$(4) \frac{24}{\sqrt{6}} - 3\sqrt{6} + \frac{15\sqrt{2}}{\sqrt{3}} = \frac{24 \times \sqrt{6}}{\sqrt{6} \times \sqrt{6}} - 3\sqrt{6} + \frac{15\sqrt{2} \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} \\ = 4\sqrt{6} - 3\sqrt{6} + 5\sqrt{6} \\ = 6\sqrt{6}$$