

## 文字と式（多項式の計算）

[1] [解答] (1)  $3x - 2y$  (2)  $7a - 6b$

$$\begin{aligned}(1) \quad (x - 3y) + (2x + y) &= x - 3y + 2x + y \\&= x + 2x - 3y + y \\&= 3x - 2y\end{aligned}$$

$$\begin{aligned}(2) \quad (5a - 2b) + (2a - 4b) &= 5a - 2b + 2a - 4b \\&= 5a + 2a - 2b - 4b \\&= 7a - 6b\end{aligned}$$

[2] [解答] (1)  $10x + 7y$  (2)  $-x + y$  (3)  $7a - 7b$  (4)  $4a + 2b$   
(5)  $5x^2 - xy$  (6)  $ab + 3bc + ca$

$$\begin{aligned}(1) \quad (3x + y) + (7x + 6y) &= 3x + y + 7x + 6y \\&= 3x + 7x + y + 6y \\&= 10x + 7y\end{aligned}$$

$$\begin{aligned}(2) \quad (2x - y) + (-3x + 2y) &= 2x - y - 3x + 2y \\&= 2x - 3x - y + 2y \\&= -x + y\end{aligned}$$

$$\begin{aligned}(3) \quad (3a - 2b) + (4a - 5b) &= 3a - 2b + 4a - 5b \\&= 3a + 4a - 2b - 5b \\&= 7a - 7b\end{aligned}$$

$$\begin{aligned}(4) \quad 8a + (-4a + 2b) &= 8a - 4a + 2b \\&= 4a + 2b\end{aligned}$$

$$\begin{aligned}(5) \quad (3x^2 - 2xy + 4y^2) + (2x^2 + xy - 4y^2) &= 3x^2 - 2xy + 4y^2 + 2x^2 + xy - 4y^2 \\&= 3x^2 + 2x^2 - 2xy + xy + 4y^2 - 4y^2 \\&= 5x^2 - xy\end{aligned}$$

$$\begin{aligned}(6) \quad (-2ab + 4bc - ca) + (3ab - bc + 2ca) &= -2ab + 4bc - ca + 3ab - bc + 2ca \\&= -2ab + 3ab + 4bc - bc - ca + 2ca \\&= ab + 3bc + ca\end{aligned}$$

[3] [解答] (1)  $-2x + y$  (2)  $2a + 3b$

$$\begin{aligned}(1) \quad (4x + 3y) - (6x + 2y) &= 4x + 3y - 6x - 2y \\&= 4x - 6x + 3y - 2y \\&= -2x + y\end{aligned}$$

$$(2) \quad (7a - 3b) - (5a - 6b) = 7a - 3b - 5a + 6b$$

$$= 7a - 5a - 3b + 6b$$

$$= 2a + 3b$$

[4] [解答] (1)  $3x + 3y$  (2)  $3a - 3b$  (3)  $2x + 11y$  (4)  $-a - 6b$   
(5)  $x^2 - 4xy - 3y^2$  (6)  $-2ab + bc$

$$\begin{aligned}(1) \quad (7x + 2y) - (4x - y) &= 7x + 2y - 4x + y \\&= 7x - 4x + 2y + y \\&= 3x + 3y\end{aligned}$$

$$\begin{aligned}(2) \quad (4a - 7b) - (a - 4b) &= 4a - 7b - a + 4b \\&= 4a - a - 7b + 4b \\&= 3a - 3b\end{aligned}$$

$$\begin{aligned}(3) \quad (5x + 4y) - (3x - 7y) &= 5x + 4y - 3x + 7y \\&= 5x - 3x + 4y + 7y \\&= 2x + 11y\end{aligned}$$

$$\begin{aligned}(4) \quad (-4a - 7b) - (-b - 3a) &= -4a - 7b + b + 3a \\&= -4a + 3a - 7b + b \\&= -a - 6b\end{aligned}$$

$$\begin{aligned}(5) \quad (6x^2 - xy - 2y^2) - (5x^2 + 3xy + y^2) &= 6x^2 - xy - 2y^2 - 5x^2 - 3xy - y^2 \\&= 6x^2 - 5x^2 - xy - 3xy - 2y^2 - y^2 \\&= x^2 - 4xy - 3y^2\end{aligned}$$

$$\begin{aligned}(6) \quad (5ab - bc + 3ca) - (7ab + 3ca - 2bc) &= 5ab - bc + 3ca - 7ab - 3ca + 2bc \\&= 5ab - 7ab - bc + 2bc + 3ca - 3ca \\&= -2ab + bc\end{aligned}$$

[5] [解答] (1)  $6x - 2y$  (2)  $-5a - 10b$  (3)  $6x - 3y + 15$

$$\begin{aligned}(1) \quad 2(3x - y) &= 2 \times 3x + 2 \times (-y) \\&= 6x - 2y\end{aligned}$$

$$\begin{aligned}(2) \quad -5(a + 2b) &= (-5) \times a + (-5) \times 2b \\&= -5a - 10b\end{aligned}$$

$$\begin{aligned}(3) \quad 3(2x - y + 5) &= 3 \times 2x + 3 \times (-y) + 3 \times 5 \\&= 6x - 3y + 15\end{aligned}$$

- [6] [解答] (1)  $14x - 35y$     (2)  $-24x + 3y$     (3)  $10a - 5b + 5$     (4)  $2x - y$   
 (5)  $-2x^2 + x - 5$

$$(1) \quad 7(2x - 5y) = 7 \times 2x + 7 \times (-5y) \\ = 14x - 35y$$

$$(2) \quad (8x - y) \times (-3) = 8x \times (-3) + (-y) \times (-3) \\ = -24x + 3y$$

$$(3) \quad 5(2a - b + 1) = 5 \times 2a + 5 \times (-b) + 5 \times 1 \\ = 10a - 5b + 5$$

$$(4) \quad \frac{1}{3}(6x - 3y) = \frac{1}{3} \times 6x + \frac{1}{3} \times (-3y) \\ = 2x - y$$

$$(5) \quad (4x^2 - 2x + 10) \times \left(-\frac{1}{2}\right) = 4x^2 \times \left(-\frac{1}{2}\right) + (-2x) \times \left(-\frac{1}{2}\right) + 10 \times \left(-\frac{1}{2}\right) \\ = -2x^2 + x - 5$$

- [7] [解答] (1)  $2x + 3y$     (2)  $-3a + 2b - 1$

$$(1) \quad (4x + 6y) \div 2 = (4x + 6y) \times \frac{1}{2} \\ = 4x \times \frac{1}{2} + 6y \times \frac{1}{2} \\ = 2x + 3y$$

$$(2) \quad (15a - 10b + 5) \div (-5) = (15a - 10b + 5) \times \left(-\frac{1}{5}\right) \\ = 15a \times \left(-\frac{1}{5}\right) - 10b \times \left(-\frac{1}{5}\right) + 5 \times \left(-\frac{1}{5}\right) \\ = -3a + 2b - 1$$

- [8] [解答] (1)  $3x - y$     (2)  $-3a + 5b$     (3)  $x + 3y - 4$     (4)  $-2x^2 + x + 4$   
 (5)  $2a - \frac{3}{2}b$

$$(1) \quad (12x - 4y) \div 4 = (12x - 4y) \times \frac{1}{4} = 3x - y$$

$$(2) \quad (9a - 15b) \div (-3) = (9a - 15b) \times \left(-\frac{1}{3}\right) = -3a + 5b$$

$$(3) \quad (2x + 6y - 8) \div 2 = (2x + 6y - 8) \times \frac{1}{2} = x + 3y - 4$$

$$(4) \quad (10x^2 - 5x - 20) \div (-5) = (10x^2 - 5x - 20) \times \left(-\frac{1}{5}\right) = -2x^2 + x + 4$$

$$(5) \quad \left(\frac{6}{7}a - \frac{9}{14}b\right) \div \frac{3}{7} = \left(\frac{6}{7}a - \frac{9}{14}b\right) \times \frac{7}{3} = 2a - \frac{3}{2}b$$

- [9] [解答] (1)  $3a + b$     (2)  $3p + 5q$     (3)  $2x - 3y$     (4)  $-3m + 2n$   
 (5)  $2a^2 + 3a$     (6)  $2x^2 + 3y^2$     (7)  $2a - 5b + 3$     (8)  $-6x - 9y + 1$   
 (9)  $8a^2 - 5a - 11$

$$(1) \quad (12a + 4b) \div 4 = (12a + 4b) \times \frac{1}{4} \\ = 3a + b$$

$$(2) \quad (6p + 10q) \div 2 = (6p + 10q) \times \frac{1}{2} \\ = 3p + 5q$$

$$(3) \quad (12x - 18y) \div 6 = (12x - 18y) \times \frac{1}{6} \\ = 2x - 3y$$

$$(4) \quad (21m - 14n) \div (-7) = (21m - 14n) \times \left(-\frac{1}{7}\right) \\ = -3m + 2n$$

$$(5) \quad (-18a^2 - 27a) \div (-9) = (-18a^2 - 27a) \times \left(-\frac{1}{9}\right) \\ = 2a^2 + 3a$$

$$(6) \quad (32x^2 + 48y^2) \div 16 = (32x^2 + 48y^2) \times \frac{1}{16} \\ = 2x^2 + 3y^2$$

$$(7) \quad (6a - 15b + 9) \div 3 = (6a - 15b + 9) \times \frac{1}{3} \\ = 2a - 5b + 3$$

$$(8) \quad (42x + 63y - 7) \div (-7) = (42x + 63y - 7) \times \left(-\frac{1}{7}\right) \\ = -6x - 9y + 1$$

$$(9) \quad (64a^2 - 40a - 88) \div 8 = (64a^2 - 40a - 88) \times \frac{1}{8} \\ = 8a^2 - 5a - 11$$

<p>[10] [解答] (1) <math>-5x + 3y</math> (2) <math>10a^2 + 6a - 2</math> (3) <math>6m - 9n + 3</math> (4) <math>6x^2 + x - 3</math>  (5) <math>2a^2 + 7a - 8</math> (6) <math>-m - 2n + 9</math> (7) <math>9x^2 - x - 6</math></p> <p>(1) <math>(20x - 12y) \times \left(-\frac{1}{4}\right) = 20x \times \left(-\frac{1}{4}\right) - 12y \times \left(-\frac{1}{4}\right)</math>  <math>= -5x + 3y</math></p> <p>(2) <math>2(5a^2 + 3a - 1) = 2 \times 5a^2 + 2 \times 3a + 2 \times (-1)</math>  <math>= 10a^2 + 6a - 2</math></p> <p>(3) <math>(4m - 6n + 2) \div \frac{2}{3} = (4m - 6n + 2) \times \frac{3}{2}</math>  <math>= 4m \times \frac{3}{2} - 6n \times \frac{3}{2} + 2 \times \frac{3}{2}</math>  <math>= 6m - 9n + 3</math></p> <p>(4) <math>(5x^2 - x) + (x^2 + 2x - 3) = 5x^2 - x + x^2 + 2x - 3</math>  <math>= 5x^2 + x^2 - x + 2x - 3</math>  <math>= 6x^2 + x - 3</math></p> <p>(5) <math>(3a^2 + 7a - 9) - (a^2 - 1) = 3a^2 + 7a - 9 - a^2 + 1</math>  <math>= 3a^2 - a^2 + 7a - 9 + 1</math>  <math>= 2a^2 + 7a - 8</math></p> <p>(6) <math>(2m + 6n + 4) - (3m + 8n - 5) = 2m + 6n + 4 - 3m - 8n + 5</math>  <math>= 2m - 3m + 6n - 8n + 4 + 5</math>  <math>= -m - 2n + 9</math></p> <p>(7) <math>(6x^2 - 2x - 5) + (3x^2 + x - 1) = 6x^2 - 2x - 5 + 3x^2 + x - 1</math>  <math>= 6x^2 + 3x^2 - 2x + x - 5 - 1</math>  <math>= 9x^2 - x - 6</math></p>	<p><math>= -a + b</math></p> <p>(4) <math>6(x - 2y) - 3(4x - 3y) = 6x - 12y - 12x + 9y</math>  <math>= 6x - 12x - 12y + 9y</math>  <math>= -6x - 3y</math></p> <p>[12] [解答] (1) <math>4x - 7y</math> (2) <math>6m + 5n</math> (3) <math>8a - 4b + 16</math>  (4) <math>-9a^2 - 15a - 1</math> (5) <math>7x - 6y - 13</math> (6) <math>3a^2 + a + 2</math></p> <p>(1) <math>5(2x - 5y) - 6(x - 3y) = 10x - 25y - 6x + 18y</math>  <math>= 10x - 6x - 25y + 18y</math>  <math>= 4x - 7y</math></p> <p>(2) <math>-8(m + 2n) + 7(2m + 3n) = -8m - 16n + 14m + 21n</math>  <math>= -8m + 14m - 16n + 21n</math>  <math>= 6m + 5n</math></p> <p>(3) <math>2(2a + 4b) + 4(a - 3b + 4) = 4a + 8b + 4a - 12b + 16</math>  <math>= 4a + 4a + 8b - 12b + 16</math>  <math>= 8a - 4b + 16</math></p> <p>(4) <math>5(a^2 - 3a + 4) - 7(2a^2 + 3) = 5a^2 - 15a + 20 - 14a^2 - 21</math>  <math>= 5a^2 - 14a^2 - 15a + 20 - 21</math>  <math>= -9a^2 - 15a - 1</math></p> <p>(5) <math>3(x - 4y - 5) + 2(2x + 3y + 1) = 3x - 12y - 15 + 4x + 6y + 2</math>  <math>= 3x + 4x - 12y + 6y - 15 + 2</math>  <math>= 7x - 6y - 13</math></p> <p>(6) <math>4(2a^2 + 4a - 2) - 5(a^2 + 3a - 2) = 8a^2 + 16a - 8 - 5a^2 - 15a + 10</math>  <math>= 8a^2 - 5a^2 + 16a - 15a - 8 + 10</math>  <math>= 3a^2 + a + 2</math></p>
<p>[11] [解答] (1) <math>6x - 5y</math> (2) <math>8a - 2b</math> (3) <math>-a + b</math> (4) <math>-6x - 3y</math></p> <p>(1) <math>(3x + y) + 3(x - 2y) = 3x + y + 3x - 6y</math>  <math>= 3x + 3x + y - 6y</math>  <math>= 6x - 5y</math></p> <p>(2) <math>4(a - 2b) + 2(2a + 3b) = 4a - 8b + 4a + 6b</math>  <math>= 4a + 4a - 8b + 6b</math>  <math>= 8a - 2b</math></p> <p>(3) <math>4(2a + b) - 3(3a + b) = 8a + 4b - 9a - 3b</math>  <math>= 8a - 9a + 4b - 3b</math></p>	

[13] [解答] (1)  $\frac{3x+2y}{4}$  (2)  $\frac{7}{6}b$  (3)  $\frac{5x-5y}{6}$

$$(1) \frac{x-4y}{4} + \frac{x+3y}{2} = \frac{x-4y}{4} + \frac{2(x+3y)}{4}$$

$$= \frac{(x-4y)+2(x+3y)}{4}$$

$$= \frac{x-4y+2x+6y}{4}$$

$$= \frac{3x+2y}{4}$$

$$(2) \frac{a+2b}{3} - \frac{2a-3b}{6} = \frac{2(a+2b)}{6} - \frac{2a-3b}{6}$$

$$= \frac{2(a+2b)-(2a-3b)}{6}$$

$$= \frac{2a+4b-2a+3b}{6}$$

$$= \frac{7}{6}b$$

$$(3) \frac{x-3y}{2} + \frac{x+2y}{3} = \frac{3(x-3y)}{6} + \frac{2(x+2y)}{6}$$

$$= \frac{3(x-3y)+2(x+2y)}{6}$$

$$= \frac{3x-9y+2x+4y}{6}$$

$$= \frac{5x-5y}{6}$$

[14] [解答] (1)  $18x+15y$  (2)  $a+4b$  (3)  $13m+n$  (4)  $14x-3y$   
 (5)  $13a-30b$  (6)  $-18x-2y$  (7)  $8a$  (8)  $9p+36q$   
 (9)  $15x^2+11x-22$  (10)  $34a^2+35ab-24b^2$

$$(1) 8x+5(2x+3y)=8x+10x+15y$$

$$=18x+15y$$

$$(2) -4(6a-b)+25a=-24a+4b+25a$$

$$=-24a+25a+4b$$

$$=a+4b$$

$$(3) 2(9m-3n)+(-5m+7n)=18m-6n-5m+7n$$

$$=18m-5m-6n+7n$$

$$=13m+n$$

$$(4) 3(2x+5y)+2(4x-9y)=6x+15y+8x-18y$$

$$=6x+8x+15y-18y$$

$$=14x-3y$$

$$(5) 3(a-5b)+5(2a-3b)=3a-15b+10a-15b$$

$$=3a+10a-15b-15b$$

$$=13a-30b$$

$$(6) 2(-5x+y)-4(2x+y)=-10x+2y-8x-4y$$

$$=-10x-8x+2y-4y$$

$$=-18x-2y$$

$$(7) 5(3a-7b)-7(a-5b)=15a-35b-7a+35b$$

$$=15a-7a-35b+35b$$

$$=8a$$

$$(8) -3(p-2q)+6(2p+5q)=-3p+6q+12p+30q$$

$$=-3p+12p+6q+30q$$

$$=9p+36q$$

$$(9) 3(x^2-7x+2)+4(3x^2+8x-7)=3x^2-21x+6+12x^2+32x-28$$

$$=3x^2+12x^2-21x+32x+6-28$$

$$=15x^2+11x-22$$

$$(10) 7(4a^2+5ab-2b^2)-2(5b^2-3a^2)=28a^2+35ab-14b^2-10b^2+6a^2$$

$$=28a^2+6a^2+35ab-14b^2-10b^2$$

$$=34a^2+35ab-24b^2$$

15 [解答] (1)  $\frac{8x+3y}{8}$  (2)  $\frac{6a-11b}{12}$  (3)  $\frac{-4x+8y}{3}$

$$(1) \frac{3x+5y}{4} + \frac{2x-7y}{8} = \frac{2(3x+5y)}{8} + \frac{2x-7y}{8}$$
$$= \frac{2(3x+5y)+(2x-7y)}{8}$$
$$= \frac{6x+10y+2x-7y}{8}$$
$$= \frac{8x+3y}{8}$$

$$(2) \frac{3a-2b}{3} - \frac{2a+b}{4} = \frac{4(3a-2b)}{12} - \frac{3(2a+b)}{12}$$
$$= \frac{4(3a-2b)-3(2a+b)}{12}$$
$$= \frac{12a-8b-6a-3b}{12}$$
$$= \frac{6a-11b}{12}$$

$$(3) \frac{2x+5y}{3} - (2x-y) = \frac{2x+5y}{3} - \frac{3(2x-y)}{3}$$
$$= \frac{2x+5y-3(2x-y)}{3}$$
$$= \frac{2x+5y-6x+3y}{3}$$
$$= \frac{-4x+8y}{3}$$