

連立方程式② 解答と解説

[1] [解答] (1) $x=7, y=2$ (2) $x=-1, y=3$ (3) $x=-3, y=7$

$$(1) \begin{cases} 2x - 3y = 8 & \dots \dots \textcircled{1} \\ x - 2y = 3 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \quad 2x - 3y = 8 \\ \textcircled{2} \times 2 \quad \underline{-} \quad 2x - 4y = 6 \\ \hline y = 2 \end{array}$$

$y=2$ を ② に代入すると

$$\begin{aligned} x - 2 \times 2 &= 3 \\ x &= 7 \end{aligned}$$

よって $x=7, y=2$

$$(2) \begin{cases} 2x - y = -5 & \dots \dots \textcircled{1} \\ -3x + 2y = 9 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \times 2 \quad 4x - 2y = -10 \\ \textcircled{2} \quad \underline{+} \quad -3x + 2y = 9 \\ \hline x = -1 \end{array}$$

$x=-1$ を ① に代入すると

$$\begin{aligned} 2 \times (-1) - y &= -5 \\ -y &= -3 \\ y &= 3 \end{aligned}$$

よって $x=-1, y=3$

$$(3) \begin{cases} 3x + y = -2 & \dots \dots \textcircled{1} \\ 5x + 3y = 6 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \times 3 \quad 9x + 3y = -6 \\ \textcircled{2} \quad \underline{-} \quad 5x + 3y = 6 \\ \hline 4x = -12 \\ x = -3 \end{array}$$

$x=-3$ を ① に代入すると

$$\begin{aligned} 3 \times (-3) + y &= -2 \\ y &= 7 \end{aligned}$$

よって $x=-3, y=7$

[2] [解答] (1) $x=2, y=-1$ (2) $x=-5, y=6$ (3) $x=3, y=-3$

(4) $x=-2, y=2$

$$(1) \begin{cases} 4x + 3y = 5 & \dots \dots \textcircled{1} \\ -2x - 5y = 1 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \quad 4x + 3y = 5 \\ \textcircled{2} \times 2 \quad \underline{+} \quad -4x - 10y = 2 \\ \hline -7y = 7 \\ y = -1 \end{array}$$

$y=-1$ を ① に代入すると

$$\begin{aligned} 4x + 3 \times (-1) &= 5 \\ 4x &= 8 \\ x &= 2 \end{aligned}$$

よって $x=2, y=-1$

$$(2) \begin{cases} 2x + 3y = 8 & \dots \dots \textcircled{1} \\ 7x + 6y = 1 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \times 2 \quad 4x + 6y = 16 \\ \textcircled{2} \quad \underline{-} \quad 7x + 6y = 1 \\ \hline -3x = 15 \\ x = -5 \end{array}$$

$x=-5$ を ① に代入すると

$$\begin{aligned} 2 \times (-5) + 3y &= 8 \\ 3y &= 18 \\ y &= 6 \end{aligned}$$

よって $x=-5, y=6$

$$(3) \begin{cases} 3x + 4y = -3 & \dots \dots \textcircled{1} \\ 9x + 5y = 12 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \times 3 \quad 9x + 12y = -9 \\ \textcircled{2} \quad \underline{-} \quad 9x + 5y = 12 \\ \hline 7y = -21 \\ y = -3 \end{array}$$

$y=-3$ を ① に代入すると

$$\begin{aligned} 3x + 4 \times (-3) &= -3 \\ 3x &= 9 \\ x &= 3 \end{aligned}$$

よって $x=3, y=-3$

$$(4) \begin{cases} 3x - 2y = -10 & \dots \dots \textcircled{1} \\ 5x + 8y = 6 & \dots \dots \textcircled{2} \end{cases}$$

$$\begin{array}{r} \textcircled{1} \times 4 \quad 12x - 8y = -40 \\ \textcircled{2} \quad \underline{+} \quad 5x + 8y = 6 \\ \hline 17x = -34 \\ x = -2 \end{array}$$

$x = -2$ を ① に代入すると

$$3 \times (-2) - 2y = -10$$

$$-6 - 2y = -10$$

$$-2y = -4$$

$$y = 2$$

よって $x = -2, y = 2$