

式と計算 (単項式と多項式の乗除) 解答と解説

1 解答 (1) $2ab + 3ac$ (2) $3x^2 - 6xy$ (3) $-2x^2 + 10x$ (4) $-12ab - 20b^2$

(1) $a(2b + 3c) = a \times 2b + a \times 3c$
 $= 2ab + 3ac$

(2) $(x - 2y) \times 3x = x \times 3x - 2y \times 3x$
 $= 3x^2 - 6xy$

(3) $-2x(x - 5) = -2x \times x - 2x \times (-5)$
 $= -2x^2 + 10x$

(4) $(3a + 5b) \times (-4b) = 3a \times (-4b) + 5b \times (-4b)$
 $= -12ab - 20b^2$

2 解答 (1) $3a^2 - 6ab + 15ac$ (2) $4x^2 - 10xy$ (3) $-6a^3 + 4a^2b - 3ab$

(1) $3a(a - 2b + 5c) = 3a \times a + 3a \times (-2b) + 3a \times 5c$
 $= 3a^2 - 6ab + 15ac$

(2) $(6x - 15y) \times \frac{2}{3}x = 6x \times \frac{2}{3}x - 15y \times \frac{2}{3}x$
 $= 4x^2 - 10xy$

(3) $-\frac{1}{4}a(24a^2 - 16ab + 12b) = -\frac{1}{4}a \times 24a^2 - \frac{1}{4}a \times (-16ab) - \frac{1}{4}a \times 12b$
 $= -6a^3 + 4a^2b - 3ab$

3 解答 (1) $xy + x$ (2) $-8ac + 12bc$ (3) $6x^2 - 3xy - 3x$

(1) $x(y + 1) = x \times y + x \times 1$
 $= xy + x$

(2) $(2a - 3b) \times (-4c) = 2a \times (-4c) - 3b \times (-4c)$
 $= -8ac + 12bc$

(3) $3x(2x - y - 1) = 3x \times 2x + 3x \times (-y) + 3x \times (-1)$
 $= 6x^2 - 3xy - 3x$

4 解答 (1) $ab + 2ac$ (2) $6x^2 - 2xy$ (3) $-3x^2 + 3x$ (4) $-20a^2 - 15ab$

(5) $3x^3 - x^2$ (6) $4a^3 - 6a^2$

(1) $a(b + 2c) = a \times b + a \times 2c$
 $= ab + 2ac$

(2) $(3x - y) \times 2x = 3x \times 2x - y \times 2x$
 $= 6x^2 - 2xy$

(3) $-3x(x - 1) = -3x \times x - 3x \times (-1)$
 $= -3x^2 + 3x$

(4) $(4a + 3b) \times (-5a) = 4a \times (-5a) + 3b \times (-5a)$
 $= -20a^2 - 15ab$

(5) $(6x^2 - 2x) \times \frac{1}{2}x = 6x^2 \times \frac{1}{2}x - 2x \times \frac{1}{2}x$
 $= 3x^3 - x^2$

(6) $-\frac{2}{3}a(-6a^2 + 9a) = -\frac{2}{3}a \times (-6a^2) - \frac{2}{3}a \times 9a$
 $= 4a^3 - 6a^2$

5 解答 (1) $3ab + 4ac - 2a$ (2) $-2x^2 + 4xy - 6x$ (3) $-6a^2 - 3ab + 9a$

(1) $a(3b + 4c - 2) = a \times 3b + a \times 4c + a \times (-2)$
 $= 3ab + 4ac - 2a$

(2) $(x - 2y + 3) \times (-2x) = x \times (-2x) - 2y \times (-2x) + 3 \times (-2x)$
 $= -2x^2 + 4xy - 6x$

(3) $(8a + 4b - 12) \times \left(-\frac{3}{4}a\right) = 8a \times \left(-\frac{3}{4}a\right) + 4b \times \left(-\frac{3}{4}a\right) - 12 \times \left(-\frac{3}{4}a\right)$
 $= -6a^2 - 3ab + 9a$

6 解答 (1) $4ab - 12a$ (2) $5x^2 + 10x$ (3) $-3ax - 7a$ (4) $2a^2 + 16ab$
 (5) $14x^2 - 21xy$ (6) $24ab - 60ac$ (7) $9m - 2n$ (8) $-3ax + 12ay$
 (9) $-7ap + 2p^2$

(1) $4a(b-3) = 4ab - 12a$
 (2) $5x(x+2) = 5x^2 + 10x$
 (3) $-a(3x+7) = -3ax - 7a$
 (4) $2a(a+8b) = 2a^2 + 16ab$
 (5) $7x(2x-3y) = 14x^2 - 21xy$
 (6) $12a(2b-5c) = 24ab - 60ac$
 (7) $-(-9m+2n) = 9m - 2n$
 (8) $-3a(x-4y) = -3ax + 12ay$
 (9) $p(-7a+2p) = -7ap + 2p^2$

7 解答 (1) $5ax + 6a$ (2) $21x^2 - 28x$ (3) $20ap - 28a$ (4) $4ax + 3ay$
 (5) $22x^2 - 2xy$ (6) $-25mn + 35n^2$ (7) $-8ax - 7bx$
 (8) $-28ab + 63b^2$ (9) $48ux + 30vx$

(1) $(5x+6) \times a = 5ax + 6a$
 (2) $(3x-4) \times 7x = 21x^2 - 28x$
 (3) $(5p-7) \times 4a = 20ap - 28a$
 (4) $(4x+3y) \times a = 4ax + 3ay$
 (5) $(11x-y) \times 2x = 22x^2 - 2xy$
 (6) $(-5m+7n) \times 5n = -25mn + 35n^2$
 (7) $(8a+7b) \times (-x) = -8ax - 7bx$
 (8) $(4a-9b) \times (-7b) = -28ab + 63b^2$
 (9) $(-8u-5v) \times (-6x) = 48ux + 30vx$

8 解答 (1) $36ax - 45bx + 27x$ (2) $14ab + 35b^2 - 21bc$ (3) $-20x^2 - 5xy + 30xz$
 (4) $-3mx - 7my + mz$ (5) $-35ac + 20bc + 65c^2$ (6) $8px - 2qx - 3rx$
 (7) $-9ac + 6bc - 12c^2$ (8) $-12x^2 + 18xy - 22xz$ (9) $54ab - 21b^2 + 12bc$

(1) $9x(4a-5b+3) = 36ax - 45bx + 27x$
 (2) $7b(2a+5b-3c) = 14ab + 35b^2 - 21bc$
 (3) $5x(-4x-y+6z) = -20x^2 - 5xy + 30xz$
 (4) $-m(3x+7y-z) = -3mx - 7my + mz$
 (5) $-5c(7a-4b-13c) = -35ac + 20bc + 65c^2$

(6) $(8p-2q-3r) \times x = 8px - 2qx - 3rx$
 (7) $(-3a+2b-4c) \times 3c = -9ac + 6bc - 12c^2$
 (8) $(6x-9y+11z) \times (-2x) = -12x^2 + 18xy - 22xz$
 (9) $(-18a+7b-4c) \times (-3b) = 54ab - 21b^2 + 12bc$
9 解答 (1) $2a+3$ (2) $-x+2$ (3) $2a+3b$ (4) $-3x-4y$

(1) $(2a^2+3a) \div a = (2a^2+3a) \times \frac{1}{a}$

$$= \frac{2a^2}{a} + \frac{3a}{a}$$

$$= 2a + 3$$

(2) $(3x^2-6x) \div (-3x) = (3x^2-6x) \times \left(-\frac{1}{3x}\right)$

$$= -\frac{3x^2}{3x} + \frac{6x}{3x}$$

$$= -x + 2$$

(3) $(8a^2+12ab) \div 4a = (8a^2+12ab) \times \frac{1}{4a}$

$$= \frac{8a^2}{4a} + \frac{12ab}{4a}$$

$$= 2a + 3b$$

(4) $(15x^2y+20xy^2) \div (-5xy) = (15x^2y+20xy^2) \times \left(-\frac{1}{5xy}\right)$

$$= -\frac{15x^2y}{5xy} - \frac{20xy^2}{5xy}$$

$$= -3x - 4y$$

6 解答 (1) $4ab - 12a$ (2) $5x^2 + 10x$ (3) $-3ax - 7a$ (4) $2a^2 + 16ab$
 (5) $14x^2 - 21xy$ (6) $24ab - 60ac$ (7) $9m - 2n$ (8) $-3ax + 12ay$
 (9) $-7ap + 2p^2$

(1) $4a(b-3) = 4ab - 12a$
 (2) $5x(x+2) = 5x^2 + 10x$
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 (7) $(8a+7b) \times (-x) = -8ax - 7bx$
 (8) $(4a-9b) \times (-7b) = -28ab + 63b^2$
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9 解答 (1) $2a+3$ (2) $-x+2$ (3) $2a+3b$ (4) $-3x-4y$

(1) $(2a^2+3a) \div a = (2a^2+3a) \times \frac{1}{a}$

$$= \frac{2a^2}{a} + \frac{3a}{a}$$

$$= 2a + 3$$

(2) $(3x^2-6x) \div (-3x) = (3x^2-6x) \times \left(-\frac{1}{3x}\right)$

$$= -\frac{3x^2}{3x} + \frac{6x}{3x}$$

$$= -x + 2$$

(3) $(8a^2+12ab) \div 4a = (8a^2+12ab) \times \frac{1}{4a}$

$$= \frac{8a^2}{4a} + \frac{12ab}{4a}$$

$$= 2a + 3b$$

(4) $(15x^2y+20xy^2) \div (-5xy) = (15x^2y+20xy^2) \times \left(-\frac{1}{5xy}\right)$

$$= -\frac{15x^2y}{5xy} - \frac{20xy^2}{5xy}$$

$$= -3x - 4y$$

10 解答 (1) $-3a+2$ (2) $6x+3y$ (3) $6a-10b$

$$(1) (24a^2b-16ab) \div (-8ab) = (24a^2b-16ab) \times \left(-\frac{1}{8ab}\right) \\ = -\frac{24a^2b}{8ab} + \frac{16ab}{8ab} \\ = -3a+2$$

$$(2) (4x^2+2xy) \div \frac{2}{3}x = (4x^2+2xy) \times \frac{3}{2x} \\ = \frac{4x^2 \times 3}{2x} + \frac{2xy \times 3}{2x} \\ = 6x+3y$$

$$(3) (-3a^2b+5ab^2) \div \left(-\frac{1}{2}ab\right) = (-3a^2b+5ab^2) \times \left(-\frac{2}{ab}\right) \\ = \frac{3a^2b \times 2}{ab} - \frac{5ab^2 \times 2}{ab} \\ = 6a-10b$$

11 解答 (1) $3a-8$ (2) $-3x-2y$ (3) $9a-15$

$$(1) (6a^2-16a) \div 2a = (6a^2-16a) \times \frac{1}{2a} \\ = \frac{6a^2}{2a} - \frac{16a}{2a} \\ = 3a-8$$

$$(2) (9x^2y+6xy^2) \div (-3xy) = (9x^2y+6xy^2) \times \left(-\frac{1}{3xy}\right) \\ = -\frac{9x^2y}{3xy} - \frac{6xy^2}{3xy} \\ = -3x-2y$$

$$(3) (3ab-5b) \div \frac{1}{3}b = (3ab-5b) \times \frac{3}{b} \\ = \frac{3ab \times 3}{b} - \frac{5b \times 3}{b} \\ = 9a-15$$

12 解答 (1) $3x+2$ (2) $2x-5y$ (3) $-3a+2$ (4) $9a+12b$ (5) $4x^2+6y^2$

$$(1) (12x^2+8x) \div 4x = (12x^2+8x) \times \frac{1}{4x}$$

$$= \frac{12x^2}{4x} + \frac{8x}{4x} \\ = 3x+2$$

$$(2) (6ax-15ay) \div 3a = (6ax-15ay) \times \frac{1}{3a} \\ = \frac{6ax}{3a} - \frac{15ay}{3a} \\ = 2x-5y$$

$$(3) (24a^2b-16ab) \div (-8ab) = (24a^2b-16ab) \times \left(-\frac{1}{8ab}\right) \\ = -\frac{24a^2b}{8ab} + \frac{16ab}{8ab} \\ = -3a+2$$

$$(4) (6a^2+8ab) \div \frac{2}{3}a = (6a^2+8ab) \times \frac{3}{2a} \\ = \frac{6a^2 \times 3}{2a} + \frac{8ab \times 3}{2a} \\ = 9a+12b$$

$$(5) (-2x^3y-3xy^3) \div \left(-\frac{1}{2}xy\right) = (-2x^3y-3xy^3) \times \left(-\frac{2}{xy}\right) \\ = \frac{2x^3y \times 2}{xy} + \frac{3xy^3 \times 2}{xy} \\ = 4x^2+6y^2$$

13 解答 (1) $7-4y$ (2) $5a+3b$ (3) $3xy-4z$ (4) $-\frac{5a}{2}+c$
 (5) $2x-8$ (6) $10y-25axy$ (7) $-12p^2+8q^2$ (8) $-6b^3+10a$

(1) $(14x-8xy) \div 2x = (14x-8xy) \times \frac{1}{2x}$

$$= \frac{14x}{2x} - \frac{8xy}{2x}$$

$$= 7 - 4y$$

(2) $(15a^2+9ab) \div 3a = (15a^2+9ab) \times \frac{1}{3a}$

$$= \frac{15a^2}{3a} + \frac{9ab}{3a}$$

$$= 5a + 3b$$

(3) $(-12xy^2+16yz) \div (-4y) = (-12xy^2+16yz) \times \left(-\frac{1}{4y}\right)$

$$= \frac{12xy^2}{4y} - \frac{16yz}{4y}$$

$$= 3xy - 4z$$

(4) $(20abc-8bc^2) \div (-8bc) = (20abc-8bc^2) \times \left(-\frac{1}{8bc}\right)$

$$= -\frac{5a}{2} + c$$

(5) $(-xy+4y) \div \left(-\frac{1}{2}y\right) = (-xy+4y) \times \left(-\frac{2}{y}\right)$

$$= 2x - 8$$

(6) $(12xy^2-30ax^2y^2) \div \frac{6xy}{5} = (12xy^2-30ax^2y^2) \times \frac{5}{6xy}$

$$= 10y - 25axy$$

(7) $(6p^3q^2-4pq^4) \div \left(-\frac{pq^2}{2}\right) = (6p^3q^2-4pq^4) \times \left(-\frac{2}{pq^2}\right)$

$$= -12p^2 + 8q^2$$

(8) $(-3ab^3+5a^2) \div 0.5a = (-3ab^3+5a^2) \div \frac{a}{2}$

$$= (-3ab^3+5a^2) \times \frac{2}{a}$$

$$= -6b^3 + 10a$$

14 解答 (1) $4x^2-x$ (2) $3x^2-10xy+6y^2$ (3) $11x-12$ (4) $5x^2-3x$

(1) $2x(x+1)+x(2x-3) = 2x^2+2x+2x^2-3x$
 $= 4x^2-x$

(2) $3x(x-2y)-2y(2x-3y) = 3x^2-6xy-4xy+6y^2$
 $= 3x^2-10xy+6y^2$

(3) $3(x^2+2x-4)-x(3x-5) = 3x^2+6x-12-3x^2+5x$
 $= 11x-12$

(4) $x(2x-1)-(6x^2-9x^3) \div 3x = 2x^2-x-(2x-3x^2)$
 $= 2x^2-x-2x+3x^2$
 $= 5x^2-3x$

15 解答 (1) $4x^2-3x$ (2) $9a^2$

(1) $2x(3x+1)-x(2x+5) = 6x^2+2x-2x^2-5x$
 $= 4x^2-3x$

(2) $3a(a-4b)+6a(2b+a) = 3a^2-12ab+12ab+6a^2$
 $= 9a^2$